



Distributions in Reliability sub-system

Birnbaum-Saunders

$$x \sim \text{dbs}(\alpha, \beta) \quad \frac{1}{\sqrt{2\pi x^3}} \frac{(x + \beta)}{2\alpha\sqrt{\beta}} \exp \left\{ -\frac{1}{2\alpha^2} \left(\frac{x}{\beta} + \frac{\beta}{x} - 2 \right) \right\}; \quad x > 0$$

Burr X (Generalized Rayleigh)

$$x \sim \text{dburrX}(\alpha, \lambda) \quad 2 \alpha \lambda^2 x e^{-(\lambda x)^2} \left\{ 1 - e^{-(\lambda x)^2} \right\}^{\alpha-1}; \quad x > 0$$

Burr XII Distribution

$$x \sim \text{dburrXII}(\alpha, \beta) \quad \alpha \beta x^{\beta-1} \left\{ 1 + x^\beta \right\}^{-(\alpha+1)}; \quad x > 0.$$

Exponential Power (Smith & Bain)

$$x \sim \text{dexp.power}(\alpha, \lambda) \quad \alpha \lambda^\alpha x^{\alpha-1} e^{(\lambda x)^\alpha} \exp \left\{ 1 - e^{(\lambda x)^\alpha} \right\}; \quad x \geq 0$$

Exponentiated Weibull

$$x \sim \text{dexp.weib}(\alpha, \theta) \quad \alpha \theta x^{\alpha-1} e^{-x^\alpha} \left\{ 1 - \exp(-x^\alpha) \right\}^{\theta-1}; \quad x > 0$$

Extended Exponential (Marshall-Olkin)

$$x \sim \text{dext.exp}(\alpha, \lambda) \quad \frac{\alpha \lambda e^{-\lambda x}}{\left\{ 1 - (1 - \alpha) e^{-\lambda x} \right\}^2}; \quad x > 0$$

Extended Weibull(Marshall-Olkin)

$$x \sim \text{dext.weib}(\alpha, \lambda) \quad \frac{\lambda \alpha x^{\alpha-1} \exp(-x^\alpha)}{\left\{1 - (1 - \lambda) \exp(-x^\alpha)\right\}^2}; \quad x > 0$$

Flexible Weibull

$$x \sim \text{dflex.weib}(\alpha, \beta) \quad \left(\alpha + \frac{\beta}{x^2}\right) \exp\left(\alpha x - \frac{\beta}{x}\right) \exp\left\{-\exp\left(\alpha x - \frac{\beta}{x}\right)\right\}; x \geq 0$$

Generalized Exponential

$$x \sim \text{dgen.exp}(\alpha, \lambda) \quad \alpha \lambda e^{-\lambda x} \left\{1 - e^{-\lambda x}\right\}^{\alpha-1}; \quad x > 0$$

Generalized Power Weibull

$$x \sim \text{dgp.weibull}(\alpha, \theta) \quad \alpha \theta x^{\alpha-1} \left(1 + x^\alpha\right)^{\theta-1} \exp\left\{1 - \left(1 + x^\alpha\right)^\theta\right\}; x \geq 0$$

Gompertz

$$x \sim \text{dgpz}(\alpha, \theta) \quad \theta e^{\alpha x} \exp\left\{\frac{\theta}{\alpha} \left(1 - e^{\alpha x}\right)\right\}; x \geq 0$$

Gumbel

$$x \sim \text{dgumbel}(\mu, \sigma) \quad \frac{1}{\sigma} \exp\left\{-\left(\frac{x - \mu}{\sigma}\right)\right\} \exp\left[-\exp\left\{-\left(\frac{x - \mu}{\sigma}\right)\right\}\right]; \quad -\infty < x < \infty$$

Inverse Gaussian

$$x \sim \text{dinv.gauss}(\mu, \lambda) \quad \sqrt{\left(\frac{\lambda}{2\pi}\right)} x^{-3/2} \exp\left\{-\frac{\lambda(x - \mu)^2}{2\mu^2 x}\right\}; x > 0$$

Inverse Weibull

$$x \sim \text{dinv.weib}(\beta, \lambda) \quad \beta \lambda^\beta x^{-(\beta+1)} \exp\left\{-\left(\frac{\lambda}{x}\right)^\beta\right\} ; x > 0$$

Linear Failure Rate

$$x \sim \text{dlin.fr}(\alpha, \beta) \quad (\alpha + \beta x) \exp\left\{-\left(\alpha x + \frac{\beta x^2}{2}\right)\right\} ; x \geq 0$$

Logistic-exponential

$$x \sim \text{dlogis.exp}(\alpha, \lambda) \quad \frac{\lambda \alpha e^{\lambda x} (e^{\lambda x} - 1)^{\alpha-1}}{\left\{1 + (e^{\lambda x} - 1)^\alpha\right\}^2} ; x \geq 0$$

Log-logistic Distribution

$$x \sim \text{dlog.logis}(\beta, \theta) \quad \frac{\beta (x/\theta)^\beta}{x \left\{1 + (x/\theta)^\beta\right\}^2} ; x > 0.$$

Log-Weibull

$$x \sim \text{dlog.weib}(\mu, \sigma) \quad \frac{1}{\sigma} \exp\left(\frac{x-\mu}{\sigma}\right) \cdot \exp\left\{-\exp\left(\frac{x-\mu}{\sigma}\right)\right\} ; -\infty < x < \infty$$

Modified Weibull

$$x \sim \text{dweib.modified}(\alpha, \beta, \lambda) \quad \alpha (\beta + \lambda x) x^{\beta-1} e^{\lambda x} \exp\left\{-\alpha x^\beta e^{\lambda x}\right\} ; x > 0$$